

# A Review on Comparative Performance Analysis of Different Digital Multipliers

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## Abstract

The importance of digital electronics is increasing day-by-day in our day-to-day life. Digital multipliers have great importance in designing modern gadgets, in digital signal processing and in many other applications. For the improvement in performance of modern devices and softwares, there is a need of designing a multiplier having high speed, less area, low power consumption, simple and regular design. Here is a review presented by comparing performance of various multipliers. The multipliers are mostly compared in terms of delay power consumption and area required etc. parameters. This paper brings all important digital multipliers together for comparative analysis. This comparative analysis helps us to select one most suitable multiplier for a particular application.

**Keywords:** digital multipliers, comparison, delay, power, area, vedic, wallce, booth.

## I. INTRODUCTION

There are many types of multiplier-architectures. Among them, (1) Array multipliers are the traditional multipliers and are analyzed for reference purposes. In addition to these, followings are the fanciest multipliers, e.g., (2) Vedic series of multipliers, (3) Booth series of multipliers, (4) Wallace-tree multipliers, (5) Dadda multiplier, and (6) Braun multiplier.

This work is divided into two phases. In 1<sup>st</sup> phase, which has series-wise comparison, we will analyze group of multipliers from a particular series separately. This is to be done to find the best one multiplier from each series. After analyzing all multipliers, we will make a list of seven multipliers out of all, which have high performance in their respective groups. These seven multipliers include the Array-multiplier for reference purpose to compare performance. In 2<sup>nd</sup> phase, which has inter-series comparison, we will compare these seven multipliers and tabulate them together. This enables us to analyze relative performance of these multipliers. This comparison helps us to select a most suitable multiplier for an application.

Now there is a list of all multipliers to be analyzed. (1) In Array multipliers, three array multipliers are taken for analysis. These are distinguished on the basis of adder used to design multiplier; (i) Array Multiplier using RCA (Ripple carry adder), (ii) using CLA (Carry Look-ahead adder), and (iii) using CSA (Carry save adder). (2) In Vedic series of multipliers, there are seven multipliers are taken for analysis, (iv) Vedic Multiplier using RCA, (v) using CLA, (vi) using CSA, (vii) using KSA (Kogge Stone Adder), (viii) using Sklansky Adder, (ix) using Brent Kung Adder, (x) using Han Carlson Adder, (3) In Booth series of multipliers, there are mainly two types of multipliers, (xi) Conventional Booth multiplier, (xii) Modified Booth multiplier, (4) In Wallace-tree multipliers, there are three multipliers; (xiii) Conventional Wallace-tree, (xiv) Modified Wallace-tree, (xv) Wallace-Booth multiplier. (5) In Dadda multipliers, (xvi) Regular dadda multipliers using RCA, (xvii) using CLA, (xviii) Partitioned dadda multipliers (xix) using RCA, (xx) using CLA. (6) In Braun multipliers, two multipliers are taken here for comparison, (xxi) using RCA, (xxii) Using KSA. Therefore, there are almost 22 multipliers to be analyzed.

### 1.1 ARRAY MULTIPLIERS

These are the conventional multipliers having regular structures. Add and shift algorithm is used for its operation and hence its circuit is based on this algorithm. By direct mapping of the manual multiplication into hardware, an Array multiplier circuit can be developed [2][14]. An array of adder circuits can be used to accumulate partial products. The partial products are generated by multiplying the multiplicand with each bit of multiplier. The bit order decides the amount of shift of partial products. At the final stage, the partial products are added. The number of generated partial products is equal to that of multiplier bits. If multiplier length is equal to N, then N-1 numbers of adders are required to implement array multiplier [3].

### 1.2 VEDIC SERIES OF MULTIPLIERS

Vedic Mathematics is an ancient system of mathematics existed in India. In this eminent approach, methods of basic arithmetic are simple, powerful and logical. Another advantage is its regularity. These advantages make Vedic Mathematics an important topic for research [4][13]. Vedic Mathematics rules are mainly based on sixteen Sutras. Out of these sixteen Sutra's Urdhva Triyakbhyam sutras and Nikhilam

sutras are used for multiplication. Vedic multipliers are considered to be the best compared with conventional multipliers and Urdhva Triyakbhyam Sutra based multiplication is more efficient compared to that of Nikhilam Sutra [20]. Implementation of Vedic mathematics on FPGA is easy due to its regularity and simplicity [4][15]. All partial products required for multiplication are calculated much before actual multiplication begins. This is the big advantage of this multiplication. Based on the Vedic Mathematics algorithm, these partial products are added to obtain final product which leads to a very high speed approach [21]. Multiplier designs based on Vedic mathematics are with high speed and consume relatively low power. Multipliers are the basic and key blocks of a Digital Signal processor. Multiplication is the key process in improving the computational speed of Digital Signal Processors [16][17]. Convolution, Fast Fourier transforms and various other transforms make use of multiplier blocks [11]. Among various methods of multiplications in Vedic mathematics, Urdhva Tiryagbhyam is efficient. Urdhva Tiryagbhyam is a general multiplication formula applicable to all cases of multiplication [17].

### **1.3 BOOTH SERIES OF MULTIPLIERS**

#### *1.3.1 Conventional Booth Multiplier*

There is no need to take the sign of the number into deliberation in dealing with unsigned multiplication. However in signed multiplication the process will be changed because the signed number is in a 2's complement pattern which would give a wrong result if multiplied by using similar process for unsigned multiplication [6]. Booth's algorithm is used for this. Booth's algorithm preserves the sign of the result. Booth multiplication allows for smaller, faster multiplication circuits through encoding the signed numbers to 2's complement, which is also a standard technique used in chip design, [6] and provides significant improvements by reducing the number of partial product to half over "long multiplication" techniques. Radix 2 is the conventional booth multiplier.

##### (i) Radix 2

In booth multiplication, partial product generation is done based on recoding scheme e.g. radix 2 encoding. Bits of multiplicand (Y) are grouped from left to right and corresponding operation on multiplier (X) is done in order to generate the partial product [19]. In radix-2 booth multiplication partial product generation is done based on encoding which is as given by Table 1. Parallel Recoding scheme used in radix-2 booth multiplier is shown in the Table 1.

#### *1.3.2 Modified Booth Multiplier*

##### (ii) Radix 4

One of the solutions attaining high speed multipliers is to improve parallelism. It helps in decreasing the number of consecutive calculation stages [31]. The Original version of Booth's multiplier (Radix – 2) had two drawbacks [07],[28]. (1). The

number of Add or Subtract operations became variable and hence became difficult while designing Parallel multipliers. (2). The Algorithm becomes disorganized when there are isolated 1s. These problems are overthrown by using Radix 4 Booth's algorithm which can browse strings of three bits with the algorithm. The above recoding has the nice feature that they translate into the partial products shown in table 2.

**Table 1.** Booth recoding for radix 2 [19]

| $Q_n$ | $Q_{n+1}$ | Recoded Booth | Operation  |
|-------|-----------|---------------|------------|
| 0     | 0         | 0             | Shift      |
| 0     | 1         | +1            | Add x      |
| 1     | 0         | -1            | Subtract x |
| 1     | 1         | 0             | Shift      |

**Table 2.** Booth recoding for radix 4 [6]

| Multiplier Bits Block |   |     | Recoded 1-bit pair |    | 2-bit booth      |                 |
|-----------------------|---|-----|--------------------|----|------------------|-----------------|
| i+1                   | i | i-1 | i+1                | i  | Multiplier Value | Partial Product |
| 0                     | 0 | 0   | 0                  | 0  | 0                | $Mx0$           |
| 0                     | 0 | 1   | 0                  | 1  | 1                | $Mx1$           |
| 0                     | 1 | 0   | 1                  | -1 | 1                | $Mx1$           |
| 0                     | 1 | 0   | 1                  | 0  | 2                | $Mx2$           |
| 1                     | 0 | 0   | -1                 | 0  | -2               | $Mx-2$          |
| 1                     | 0 | 1   | -1                 | 1  | -1               | $Mx-1$          |
| 1                     | 1 | 0   | 0                  | -1 | -1               | $Mx-1$          |
| 1                     | 1 | 0   | 0                  | 0  | 0                | $Mx0$           |

### (iii) Radix 8

Radix-8 Booth recoding is based on the same algorithm as that of Radix-4. But in radix 8, we take quartets of bits instead of triplets [27][1]. This algorithm reduces the number of partial products to  $n/3$ , where  $n$  is the number of multiplier bits. Thus it allows a gain in time in the partial products summation. Radix 8 booth encoding multiplier uses 4-bit encoding scheme. But the circuit complexity increases as compared to previous version. Radix-8 booth multiplier also lacks in most parameter like delay, speed from radix 4 booth multiplier due to the complexity of the circuit. Radix-8 booth multiplier which scan strings of four bits. An algorithm similar

to previous radix algorithm is made for radix8 booth multiplier. After encoding the multiplier the resulting partial product will be  $0, y, +2y, +3y, +4y, -4y, -3y, -2y, -y$  where  $y$  represent the multiplicand. We have to represent all the no. in 2's complement form [28].

(iv) Radix 16

For binary radix-16 Booth recoded multipliers has the maximum height of the partial product columns equal to  $\lceil n/4 \rceil$  for  $n = 64$ -bit unsigned operands can be done [26] [29].

(v) Radix-32

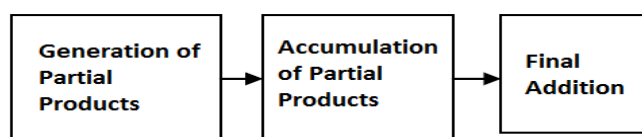
Radix32 booth multiplier reduces the no. of partial products by one fifth. An algorithm similar to previous radix algorithm is made for radix 32 booth multiplier [28].

**1.4 WALLACE-TREE SERIES OF MULTIPLIERS**

The Wallace tree method is used for implementing high speed designs. Two rows of partial products are produced that can be added in the last stage [27]. There is a reduction in critical path and the number of adders when compared to the conventional parallel adders. The Wallace tree structure can be with 3:2 compressors and 4:2. In this regard, we can expect a significant reduction in amount of computing in multiplications [27].

*1.4.1 Conventional Wallace-Tree Multiplier*

In terms of performance characteristics, designing a multiplier by using wallace tree architecture is superior over other architectures [22]. A multiplier designed by using wallace tree architecture is known as a wallace multiplier. As compared to other multiplier architectures, Wallace multiplier consumes less power and its switching speed is faster. Due to the intense interest of researchers in wallace multiplier, as result of which, different architectures are introduced to design a better wallace multiplier architecture. A conventional wallace multiplier and a reduced complexity wallace (RCW) multiplier are two architectures among them [22].



**Fig.1.** Block diagram of wallace-tree multiplier [22]

### 1.4.2 Modified Wallace-Tree Multiplier

To reduce the complexity of the reduction tree, Waters and Swartzlander presented a modification in the Traditional Wallace (TW) multiplier [23]. In this the partial products are readjusted in a reverse pyramid style. It makes it easy to analyze the tree for efficient reduction. The number of stages for RCW multiplier remains the same as that of TW multiplier. RCW tries to reduce the partial product tree using only full adders and half adders are used only where they are necessary to satisfy the number of rows in a stage. This approach enables RCW multiplier to reduce the area of the reduction process. However, a much larger final adder as compared to TW multiplier is used in RCW multiplier [23]. The size of the final adder for an  $N$ -bit RCW multiplier can be computed by: Final Adder (RCW) =  $2N - 2$ .

### 1.4.3 Wallace-Booth Multiplier

Booth recoding algorithm and compressor adders are used in Booth Recoded Wallace Tree Multiplier for its realization [24]. In this architecture, two major things with differences are that Booth Recoding algorithm is introduced to generate and reduce the number of the partial products of multiplier, whereas, 3:2, 4:2, and 5:2 compressor structures are introduced to reduce the number of partial product addition stages. Critical delay path is minimized by replacing the XOR blocks with multiplexer blocks in these compressors. Using Carry Select Adder final two rows are summed to produce the final result. This architecture has the advantage of higher speed and lower area [25].

## 1.5 DADDA MULTIPLIER

The summation proceeds in a more regular way but slower manner in array multiplication scheme. Using array scheme, at each stage of the summation only one row of bits in the matrix is eliminated [12]. The partial products are generated by using array of AND gates in a parallel multiplier. The main concern is about the summation of the partial products, and the time taken to perform this summation determines the maximum speed at which a multiplier can operate. The Dadda scheme minimizes the number of adder stages required to perform the summation of partial products. This is achieved by using half and full adders. The task is to reduce the number of rows in the matrix number of bits at each summation stage [12]. Dadda multiplier is a refinement of the parallel multipliers presented by Wallace [30].

## 1.6 BRAUN MULTIPLIER

Braun multiplier is a basic parallel multiplier. It is also called as carry save array multiplier. It is easy to design one and there is no need of logic registers. The structure consists of adders arranged in the iterative way and array of AND gates. This can be called as non-additive multipliers [5]. In the internal structure, two main things are that each products can be generated in parallel with the AND gates, and each partial

product can be added with the sum of partial product which has previously produced by using the row of adders.

The carry out will be shifted one bit to the left or right and then it will be added to the sum which is generated by the first adder and the newly generated partial product. Because the sum and carry signals are both in the critical path, in the multiplier array a full adder with balanced carry and sum delays are desirable. The main disadvantages of Braun multiplier are two; (i) the number of components required in building blocks of Braun Multiplier increases quadratically with the number of bits; (ii) at the last stage of full adders, the potential susceptibility to Glitching problems is due to exploitation of the Ripple Carry Adder (RCA) [32].

**II. PHASE- 1 (SERIES-WISE COMPARISON)**

**2.1 COMPARISION SUMMARY OF VEDIC MULTIPLIERS**

After having analysis of table 3, table 4, table 6 and table 7 got the comparison idea which shows that Vedic multiplier using HCA (han carlson adder) is the best multiplier among the vedic series of multipliers. In addition to this, table 5 is also showing a better vedic multiplier using skalansky adder.

**Table 3.** [4] Vedic Urdhava multiplier

| <b>Multipliers</b>                  | <b>Delay (ns)</b> | <b>No. of Slices</b> |
|-------------------------------------|-------------------|----------------------|
| 8-bit Urdhava                       | 12.588            | 133 out of 46560     |
| 8-bit Urdhava with mux based adder  | 9.130             | 107 out of 46560     |
| 16-bit Urdhava                      | 20.338            | 742 out of 46560     |
| 16-bit Urdhava with mux based adder | 16.994            | 594 out of 46560     |

**Table 4.** vedic multipliers [4]

| <b>Multipliers</b> | <b>%age improvement in speed</b> | <b>%age improvement in area</b> |
|--------------------|----------------------------------|---------------------------------|
| 8-bit              | 27.47%                           | 19%                             |
| 16-bit             | 16.44%                           | 20%                             |

**Table 5.** delay comparison [11]

| <b>Methode</b>                        | <b>Logic (ns)</b> | <b>Route (ns)</b> | <b>Toatl Delay(ns)</b> |
|---------------------------------------|-------------------|-------------------|------------------------|
| Vedic mul. With 8-bit RCA             | 15.717            | 10.136            | 25.853                 |
| Vedic mul. With 8-bit Skalansky adder | 14.963            | 9.351             | 24.314                 |

**Table 6.** Different vedic multipliers [21]

| No. of Bits | Adder | Delay (ns) | Slices | LUTs |
|-------------|-------|------------|--------|------|
| 6-bit       | RCA   | 15.527     | 7      | 12   |
|             | KSA   | 15.407     | 7      | 12   |
|             | HCA   | 14.052     | 8      | 14   |
| 12-bit      | RCA   | 24.963     | 14     | 24   |
|             | KSA   | 18.497     | 25     | 43   |
|             | HCA   | 17.070     | 22     | 39   |
| 24-bit      | RCA   | 44.355     | 28     | 48   |
|             | KSA   | 27.921     | 79     | 139  |
|             | HCA   | 20.196     | 59     | 104  |

**Table 7.** Comparison of various vedic multipliers [20]

COMPARISON OF COMBINATIONAL DELAY WITH  
DIFFERENT ADDER ARCHITECTURE

| Device Name                      | Multiplier | Adder Type and Combinational delay in ns |        |        |
|----------------------------------|------------|--|--------|--------|
|                                  |            | RCA                                      | CLA    | KS     |
| Spartan II<br>Xc2S200pq<br>208-5 | 4 bit      | 23.439                                   | 24.508 | 10.334 |
|                                  | 8 bit      | 42.479                                   | 42.820 | 40.176 |
|                                  | 16 bit     | 80.688                                   | 78.665 | 69.648 |
| Virtex2<br>Xc2V250F<br>G256-5    | 4 bit      | 12.964                                   | 14.553 | 13.281 |
|                                  | 8 bit      | 24.442                                   | 24.677 | 22.090 |
|                                  | 16 bit     | 45.227                                   | 41.447 | 37.184 |
| Virtex5<br>Xc5VLX22<br>0-2ff1760 | 4 bit      | 06.712                                   | 06.828 | 07.718 |
|                                  | 8 bit      | 12.214                                   | 10.864 | 05.640 |
|                                  | 16 bit     | 19.201                                   | 20.478 | 18.995 |

## 2.2 COMPARISION SUMMARY OF BOOTH MULTIPLIERS

It is obvious from theory that the modified booth multipliers with high radix are more efficient than conventional booth multipliers. It is obvious from table 9 & 10 that increase in area and delay is not that much high as the efficiency. If we compare delay



and area both simultaneously then booth with Radix 4 is the best multipliers among the booth series of multipliers.

**Table 8.** Comparison between booth radix2 & radix 4 [6]

| Device Utilization Summary                | Radix 2 | Radix 4 |
|---|---------|---------|
| Number of Slices                          | 397     | 71      |
| Number of 4 input LUTs                    | 184     | 100     |
| Number of bonded INPUT                    | 16      | 16      |
| Number of bonded OUTPUT                   | 16      | 16      |
| <b>Macro Statistics</b>                   |         |         |
| # Latches                                 | 24      | 12      |
| 8-bit latch                               | 24      | 12      |
| # Xors                                    | 71      | 23      |
| 1-bit xor2                                | 64      | 21      |
| 8-bit xor2                                | 7       | 2       |
| <b>Timing Summary</b>                     |         |         |
| Minimum period:                           | 5.454ns | 4.750ns |
| Minimum input arrival time before clock   | 7.936ns | 4.014ns |
| Maximum output required time after clock: | 6.216ns | 6.205ns |

**Table 9.** Area comparison [28]

| S.NO | BOOTH MULTIPLIER | NO. OF CELLS | TOTAL AREA |
|------|------------------|--------------|------------|
| 1    | RADIX 2          | 9426         | 27569      |
| 2    | RADIX 4          | 1690         | 3959       |
| 3    | RADIX8           | 2280         | 4359       |
| 4    | RADIX16          | 14672        | 32973      |
| 5    | RADIX32          | 25703        | 57091      |

**Table 10.** Delay comparison [28]

| S.NO | BOOTH MULTIPLIER | TIME DELAY(ns) |
|------|------------------|----------------|
| 1    | RADIX 2          | 23.382         |
| 2    | RADIX 4          | 13.993         |
| 3    | RADIX8           | 14.810         |
| 4    | RADIX16          | 26.581         |
| 5    | RADIX32          | 27.729         |

### 2.3 COMPARISION SUMMARY OF WALLACE-TREE MULTIPLIERS

From tables, it is clear that the modified booth wallace is better than the conventional wallace tree multiplier. But booth-recoded wallace tree multiplier is the most optimized multiplier. Modified wallace multiplier is better than the traditional wallace multiplier in terms of complexity and delay.

**Table 11.** Complexity of reduction[25]

| Input Size (N)          | 8   | 16   | 24   | 32   | 64    |
|-------------------------|-----|------|------|------|-------|
| Stages (S)              | 4   | 6    | 7    | 8    | 10    |
| <b>Wallace</b>          |     |      |      |      |       |
| Full adders             | 38  | 200  | 488  | 96   | 3850  |
| Half adders             | 15  | 52   | 100  | 156  | 430   |
| Total gates             | 402 | 2008 | 4801 | 8778 | 36388 |
| <b>Modified Wallace</b> |     |      |      |      |       |
| Full adders             | 39  | 201  | 490  | 907  | 3853  |
| Half adders             | 3   | 9    | 16   | 23   | 53    |
| Total gates             | 363 | 1845 | 4474 | 8263 | 34889 |

**Table 12.** Comparison number of transistor and latency[24]

| Wallace Multiplier Architectures             | Number of Transistors (N) | Latency (L) |
|--|---------------------------|-------------|
| Conventional Wallace Multiplier              | 2998                      | 27          |
| Efficient High speed Wallace Tree Multiplier | 2748                      | 15          |

Table 13. comparison of area, delay and power for wallace-tree multiplier of different sizes [23]

| Size | Delay (ns) |       |       |       | Area ( $\mu\text{m}^2$ ) |        |        |        | Power (mW) |        |        |        |
|------|------------|-------|-------|-------|--------------------------|--------|--------|--------|------------|--------|--------|--------|
|      | TW         | RCW   | Dadda | PW    | TW                       | RCW    | Dadda  | PW     | TW         | RCW    | Dadda  | PW     |
| 8    | 2.81       | 2.64  | 2.64  | 2.66  | 3392                     | 3346   | 3262   | 3148   | 1.92       | 2.04   | 1.94   | 1.96   |
| 16   | 4.13       | 3.65  | 3.80  | 3.75  | 14847                    | 14372  | 14242  | 13876  | 11.09      | 11.41  | 11.22  | 11.20  |
| 24   | 4.64       | 4.58  | 4.62  | 4.44  | 34337                    | 33479  | 33323  | 32352  | 27.69      | 28.24  | 28.32  | 28.04  |
| 32   | 14.83      | 14.62 | 14.82 | 14.62 | 61526                    | 59271  | 59086  | 58375  | 51.85      | 52.74  | 53.11  | 52.48  |
| 64   | 22.88      | 21.57 | 21.98 | 21.62 | 246842                   | 238843 | 238597 | 237553 | 216.50     | 219.17 | 222.64 | 218.92 |

**Table 14.** Delay comparison [25]

| Type             | Width (bit) | Delay (ns) |
|------------------|-------------|------------|
| Wallace          | 8           | 7.168      |
| Vedic            | 16          | 13.452     |
| Booth radix 8    | 32          | 12.081     |
| Booth radix 8    | 32          | 11.564     |
| FPGA(XC6vlx75tl) | 32          | 11.238     |
| Booth radix 8    | 32          | 9.536      |

**2.4 COMPARISION OF DADDA & BRAUN MULTIPLIERS**

Table 16 and table 17 show that partitioned dadda multiplier is better than the regular multiplier if implemented in higher order bits. For example, 64x64 partitioned multiplier is better in terms of area and delay. But it is not power efficient multiplier. Braun multiplier using Kogge stone adder (KSA) is more fast than that by using ripple carry adder (RCA).

**Table .15.** Delay for braun multipliers [32]

| S.No. | FPGA                         | Braun Multiplier using R C A (ns) | Braun Multiplier using K S A (ns) |
|-------|------------------------------|-----------------------------------|-----------------------------------|
| 1     | Spartan 2(xc2s 15-6cs144)    | 16.019                            | 15.929                            |
| 2     | Spartan 2(xc2s 200-5fg 56)   | 18.446                            | 18.346                            |
| 3     | Spartan 2E(xc2s 100e-7ft256) | 14.251                            | 14.161                            |

**Table 16.** Regular Dadda mul. With CLA [10]

| Multiplier NxN | Area( $\mu\text{m}^2$ ) | Delay(ns) | Power( $\mu\text{W}$ ) |
|----------------|-------------------------|-----------|------------------------|
| 8x8            | 8.428                   | 3.40      | 6.32                   |
| 16x16          | 29.169                  | 4.71      | 33.09                  |
| 32x32          | 105.237                 | 5.92      | 210.50                 |
| 64x64          | 397.146                 | 7.54      | 925.92                 |

**Table 17.** Partitioned Dadda mul. With CLA [10]

| Multiplier NxN | Area( $\mu\text{m}^2$ ) | Delay(ns) | Power( $\mu\text{W}$ ) |
|----------------|-------------------------|-----------|------------------------|
| 8x8            | 8.957                   | 3.51      | 6.85                   |
| 16x16          | 30.241                  | 4.61      | 35.22                  |
| 32x32          | 107.362                 | 5.47      | 218.76                 |
| 64x64          | 386.629                 | 6.94      | 952.59                 |

### III. PHASE- 2 (INTER-SERIES COMPARISON)

On the basis of comparison summaries, it is obvious that there are six better multipliers out of total 23 multipliers discussed here. Those are listed as: among vedic series (i) vedic multiplier using han carlson adder is the best, (ii) vedic multiplier using sklansky adder is also a better one. Among the booth series multipliers (i) booth radix 4 than other radix multipliers. Among wallace-tree multipliers (i) wallace-booth and (ii) modified wallace multipliers are better. Now there is a need of inter-series comparison for the analysis of relative performance of these multipliers. Now here are some tables to do this comparison.

**Table 18.** 24x24 multipliers delay, area and power comparison [8],

| Parameter                          | Array Multiplier | Booth Mul. Radix 4 | Vedic Multiplier | Wallace tree Multiplier |
|------------------------------------|------------------|--------------------|------------------|-------------------------|
| Delay(ns)                          | 19.1             | 6.35               | 8.0              | 10.6                    |
| Area                               | 96582            | 80196              | 71946            | 103847                  |
| Power dissipation( $\mu\text{W}$ ) | 18.692           | 38.529             | 20.305           | 32.932                  |
| AD( $10^{-3}$ )                    | 1.845            | 0.509              | 0.575            | 1.101                   |
| PD( $10^{-12}$ )                   | 357.0172         | 244.66             | 162.44           | 349.08                  |
| Power Ddnsity( $10^{-7}$ )         | 1.935            | 4.804              | 2.822            | 3.171                   |

**Table 19.** Comparison of 12x12 multipliers [2]

| TYPE          | DELAY (ns) | AREA | POWER (uW) | Area-Delay product( $10^3$ ) |
|---------------|------------|------|------------|------------------------------|
| ARRAY MUL     | 7.106      | 807  | 23.98      | 5.734                        |
| BOOTH radix 2 | 4.89       | 1175 | 38.264     | 5.745                        |
| BOOTH radix 4 | 4.669      | 772  | 26.22      | 3.604                        |
| WALLACE       | 4.860      | 956  | 29.209     | 4.646                        |
| BOOTH WALLACE | 4.665      | 859  | 28.830     | 4.007                        |

**Table 20.** Comparison 24x24 multipliers [9]

| Parameter                  | Array Multiplier | Booth Mul. Radix 4 | Vedic Multiplier | Wallace tree Multiplier |
|----------------------------|------------------|--------------------|------------------|-------------------------|
| Delay(ns)                  | 18.8             | 11.3               | 12.5             | 13.7                    |
| Area                       | 87707            | 46982              | 55999            | 70962                   |
| Power dissipation(uW)      | 15.878           | 12.386             | 10.299           | 15.035                  |
| AD( $10^{-3}$ )            | 1.649            | 0.531              | 0.700            | 0.972                   |
| PD( $10^{-12}$ )           | 298.5064         | 139.9618           | 128.7375         | 205.9795                |
| Power Ddnsity( $10^{-7}$ ) | 1.810            | 2.636              | 1.840            | 2.119                   |

The generalized comparison of various multipliers is shown in the table no. 21.. The lowest delay is of booth-wallace multiplier. The least areas are of modified booth and vedic multipliers. And the lowest power is of vedic multiplier. However modified booth is also a power efficient multiplier.

**Table 21.** Comparison table for conclusion

| TYPE           | DELAY   | AREA    | POWER   |
|----------------|---------|---------|---------|
| ARRAY MUL      | highest | large   | highest |
| MODIFIED BOOTH | medium  | less    | low     |
| VEDIC MUL      | medium  | less    | lowest  |
| WALLACE        | high    | large   | high    |
| BOOTH WALLACE  | low     | largest | high    |

#### IV. CONCLUSION

From the analysis of all multipliers, it is obvious that modified booth radix4 and modified wallace-booth multipliers are the best multipliers. In some cases, vedic and dadda mutipliers(in terms of speed) are also superior to these but by overall analysis booth and wallace tree can be easily modified to obtain a best optimised multiplier. This comparison helps us to select a suitable multiplier for a particular task or application. For future research, a better multiplier can be proposed by modifying these multipliers and a better comparison of various multipliers with the proposed modified multiplier can be done by taking all multipliers simultaneously in one table. That will give more accurate comparison in percentage values.

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