

## Channel and Source Coding Applied in the Bit Stream with Optimization in the Bit Rate Using Pattern Search (PS)

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### Abstract

The use of optimization techniques take lot of attention in many applications to solve research problems. In case of transmission using channel coding techniques there is no guarantee that make us sure about the selected parameters if they are adaptive to the channel noise, which make us confused about the technique that can be used to select the parameters. In this paper we are going to use the Pattern Search (PS) Algorithm technique to select the parameter of the channel coding using suitable objective function.

**Keywords:** CRC code; UEP; RS code ;SPIHT;PS; BSC

### INTRODUCTION

The specific choice of transformation type, quantization and entropy coding leads to a wide coder's variety. Numerous compression schemes have been proposed and standardized: for example, conventional compression algorithms, more sophisticated methods have been defined. Thus, in the DWT case, several compression algorithms have been developed such as "Set Partitioning In Hierarchical Trees" (SPIHT) [1], this algorithm makes it possible to progressively transmit images. We will, in what follows, present the principle of this progressive transmission.

We will then propose the unequal protection application of the bit stream with Optimization of the bit rate allocation between source coding and channel coding. Two optimization criteria will be presented: Quadratic Mean Error (MSE), peak signal-to-noise ratio (PSNR). The developed optimization method will be applied to the SPIHT encoder for source image compression

### IMAGES PROGRESSIVE TRANSMISSION

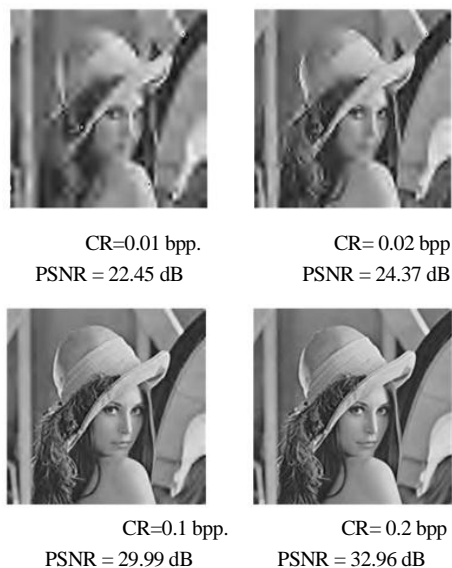
Let's start by introducing some definitions relating to the images progressive transmission [2] [3]. A bit frame at the image encoder output is said to be progressive if it can be decoded at different compression ratios, resulting in an improvement in the obtained image quality, as bits are added additionally. A binary frame is said embedded in a second binary frame if it is a prefix of the latter. An image encoder is said to be progressive if it produces, for each transmission

rate, a progressive bit frame. Images encoding is called embedded coding if the produced frame for a given bit rate is nested in the produced frame for any other higher value bit rate. It is clear that a nested images encoding is necessarily progressive. (Fig. 1) illustrates the concept of progressivity by showing a series of decoded images from the same bit frame at increasing rates ranging from 0.01 bpp to 0.2 bpp. It is obvious that higher is the bit rate, better is the visual quality of the rendered image.

In what follows, we will develop more explicitly the progressivity aspect in an image transmission [1] [4] [5]. To do this, let us begin by reminding ourselves that the main objective of a progressive transmission scheme is to transmit first the information generating the greatest reduction in distortion. Let us note the pixels set of the original image where  $i$  and  $j$  denote the pixel coordinates, and the used transformation. The transformed image is:

$$Y = \tau(X) \quad (1)$$

The matrix  $Y$  has the same dimensions as the matrix  $X$  representing the source image. Each element is called coefficient of the transform at coordinates  $(i, j)$ . The coding algorithm applies directly to the transformed image  $Y$ .



**Figure 1:** Illustration the concept of progressivity coding of the (Lena)  $512 \times 512$  image using SPIHT algorithm.

In the progressive transmission case, the decoder starts by initializing the reconstruction matrix to zero. Then, it updates the matrix components according to the decoded message. As it determines the values (exact or approximate) of certain coefficients, the decoder is able to obtain a reconstructed image:

$$\hat{X} = \tau^{-1}(\hat{Y}) \quad (2)$$

Using the mean squared error (MSE) as a distortion measurement, we have

$$D_{MSE}(X, \hat{X}) = \frac{\|X - \hat{X}\|^2}{N} = \frac{1}{N} \sum_i \sum_j (x_{i,j} - \hat{x}_{i,j})^2 \quad (3)$$

where N is the pixels number in the image. Assuming that the transformation preserves the Euclidean distance, we can write:

$$D_{MSE}(X, \hat{X}) = D_{MSE}(Y, \hat{Y}) = \frac{1}{N} \sum_i \sum_j (y_{i,j} - \hat{y}_{i,j})^2 \quad (4)$$

Thus, the exact restitution of a transform coefficient leads to the MSE reduction of  $\frac{|y_{i,j}|^2}{N}$ . As a result, in a progressive transmission scheme, the higher amplitude coefficients must be transmitted first because they generate the greatest decreases in distortion. In the same spirit, the contained information in the amplitude  $|y_{i,j}|$  of a coefficient can be distributed between the different bits constituting the binary  $|y_{i,j}|$  representation of and varies according to the nature of these bits. Indeed, the most significant bits (MSBs) provide more information on the coefficient value than the other bits. They must therefore be transmitted first.

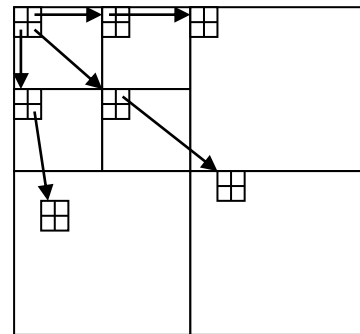
This is the principle used in bitmap coding techniques for progressive transmission.

**SPIHT ALGORITHM**

The SPIHT algorithm [1] takes the principles mentioned in EZW [2] while proposing to recursively partition the coefficient trees (Fig. 2). Thus, where EZW coded an isolated insignificant coefficient ('Z')[6], SPIHT performs a recursive partitioning of the tree in order to determine the significant coefficients position in the progeny of the considered coefficient. The significant coefficients are coded in a similar way to EZW: their sign is sent as soon as they are identified as significant and they are added to the coefficients list to be refined. This algorithm also works by bit planes [7]. It offers remarkable performances, reaching those of EZW without entropy coding. Adding entropy coding of the significance information, an additional gain between 0.3 and 0.6 dB is

obtained. The bits sent during the significance pass correspond to the program executed at the encoder during the execution of the classification algorithm into significant and insignificant coefficients. By following the same program, the decoder remains synchronous with the decisions of the encoder and finds the same classification [8]. This algorithm is based on the management of three lists, significant coefficients (LSP), insignificant coefficients (LIP) and insignificant sets (LIS). With a significance threshold divided by two at each iterations, and whose initial value is transmitted to the decoder, the algorithm proceeds as follows [9].

The significant coefficients list is initially empty, while the insignificant coefficients list contains the roots of each tree (coefficients of the low band) and the descendants of each tree. This initial partition is segmented recursively by means of two rules. If a set of descendants of a node is significant, it is separated into four direct child coefficients of this node, and all the other descendants.



**Figure 2:** Tree structure of wavelet coefficients in the case of SPIHT

Direct threads are added to the LIP or LSP according to their significance. If at least one element of all other descendants is significant, this set is separated into four insignificant sets added to the LIS. Processing the coefficients in groups of four allows efficient entropy coding thereafter. As in EZW, the refinement pass consists of progressively coding the least significant bits of the significant coefficients.

When the complexity increase due to the entropy coder use is not limiting, contextual adaptive arithmetic coding of the significance bits is possible to improve the compression performance. The coefficients being coded in four groups, it is interesting to treat them globally to exploit an entropy of order greater than 1. The coefficients can only pass from the insignificant state to the signifying state, the size of the necessary alphabet to represent these changes varies according to the number of coefficients already signifying in the group.

Thus, it is proposed in [1] to use four contexts as a function of the insignificant coefficients number varying from 1 to 4, respectively conditioning a law on an alphabet of 2 to 16 symbols. The sign bits as well as the refinement bits are not compressed, their entropy being already close to 1.

**PATTERN SEARCH CONVERGENCE**

The convergent of PS (pattern-search) method was proposed by Yu, who proved that it converged using the theory of positive bases [10]. Later, coauthors , Lagarias, and Torczon,[11-12] used positive-basis techniques to prove the convergence of another PS method, on a specific class of functions. Outside of such classes, the PS is a heuristic that can provide useful approximate solutions for many problems, but can fail on others. Outside of such classes, PS is't an iterative method that converges to the solution; indeed, the PS methods can converge to non stationary points on some relatively tame problems [13-14].

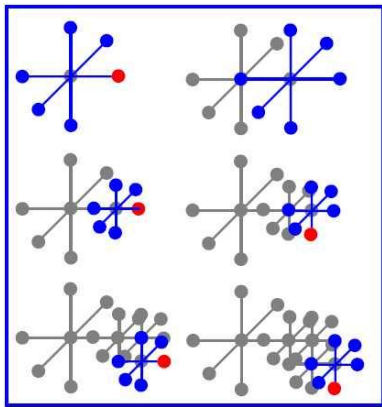


Figure 3: Pattern search convergence

**OPTIMIZATION FOR CHANNELS WITHOUT MEMORY**

In image transmission systems designing, there is often a major problem of ensuring high robustness against transmission errors while maintaining a high spectral efficiency of the system. This results in a compromise made in the system parameters choice between a very strong compression resulting in a low bit rate at the output of the source code and a very strong protection against errors obtained by low yield channel coding means. In the channel without memory case, it is assumed that the average error rate on the channel as well as its bandwidth will impose a maximum transmission rate. Knowing the maximum number of bits allowed per image, it is important to carefully choose the source encoder compression rate and the channel encoder output in order to have a reconstructed image with the best possible quality. It should be noted that reducing the channel coding efficiency, of course, gives better protection against errors, but the overall transmission rate being fixed, it is then necessary to increase the compression at the level of the source coding which results in a PSNR decrease in the first time with errors absence. Therefore, the channel coding efficiency adjustment must be done in such a way as to avoid wasting bits creating unnecessary redundancy, preserving a sufficiently low error probability after decoding. The problem is to find an optimal bit rate allocation between the source coding and the channel coding for a given transmission channel.

**A. Performance RS code**

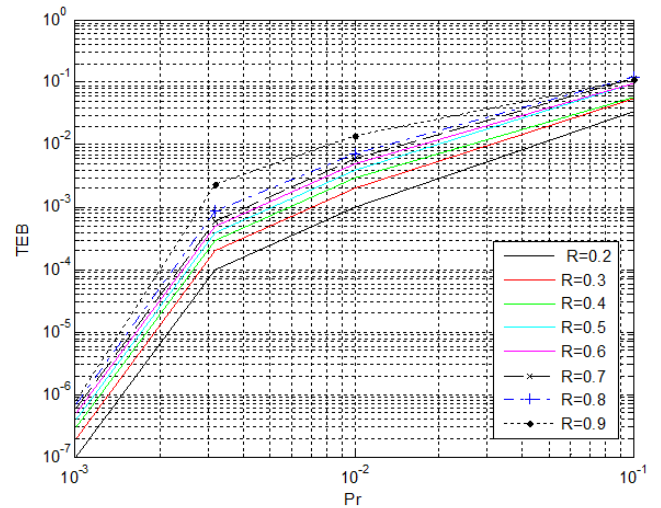


Figure 4: error Bit rate in function of error probability.

The different encoder performance is represented: the bit error rate as a function of the channel error probability, in Figure 4.

**PROTECTION OF SPIHT ENCODED IMAGES BY REED SOLOMON CODE (RS)**

**A. Description of the coding scheme**

In what follows, we propose the reed solomon (RS) code application for the protection of images coded by the SPIHT algorithm (with arithmetic coding). The block diagram of the transmission chain under consideration is shown in

Fig.4.

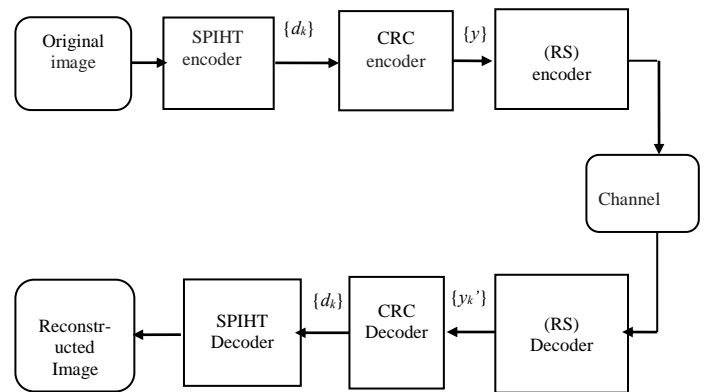


Figure 5: Block diagram of the transmission

The data delivered by the SPIHT encoder is partitioned into consecutive blocks of size  $(R_i-16)$  bits each. It is assumed that the channel coding strategy is done in two steps: error-detecting coding (CRC) followed by error-correcting coding (reed Solomon RS). The role of error detection is to interrupt

the decoding of the first detected error and therefore to reject the bits that can contribute to the propagation of errors. At the receiver, the decoding is stopped at the first detected erroneous packet, since the following packets are generally unable to improve the quality of the decoded picture. The CRC encoder adds 16 redundancy bits to each block.

The resulting data is transmitted on a channel without memory. At the receiver, a decoding (RS) is performed at the output of the channel (in the case of a symmetrical binary channel). The use of these codes makes it possible to have very high coding efficiencies giving rise to a better spectral efficiency of the system.

**B. Choice of coding performance and results on a BSC**

In what follows, we will discuss the problem of adjusting the channel coding efficiency for a given transmission channel error probability. For this, we consider a set of Code Rates obtained for EEP and UEP protection:

{0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9}. The manual UEP protection system is tested with RS on "Lena" and "Goldhill" images of size 512x512. A Symmetric Binary Channel (BSC) with two BERs:  $10^{-2}$ , and  $10^{-3}$  is considered. The selection of the reed solomon (RS) code to be applied for each BER of the channel is done experimentally. Indeed, the code (RS) is applied to obtain the highest efficiency, a global bit rate (including source coding and channel coding) of 0.25 to show the (RS) used.

In Figure 6 and Figure 7 we provided some results of decoded images with EEP and UEP protection, in order to illustrate the improvement brought by the application of RS at the visual quality level of the images transmitted on a Symmetric binary error rate channel  $10^{-2}$ , or  $10^{-3}$ .



**Figure 6:** Recieved image (Lena) with EEP and UEP protection transmitted in BSC channel (CR = 0.25 bpp).



**Figure 7:** Recieved image (Goldhill) with EEP and UEP protection transmitted in BSC channel (CR = 0.25 bpp).



**C. Joint optimization of bit rate allocation between source coding and channel coding**

This first study allowed us to highlight the efficiency of a channel coding scheme, using the reed solomon (RS) code, for the protection of SPIHT coded images transmitted over a symmetric binary channel. In what follows, we will study in more detail the problem of joint optimization of the rate allocation between a nested source encoder and any channel encoder.

**D. Coding and transmission process**

We are interested in encoding and transmitting, on a noisy channel without a given memory, a bit frame delivered by a nested source encoder, coding an HS number of source symbols. It is assumed that the channel coding strategy is done in two steps: error-detection coding followed by error-correcting coding. The role of error detection is to interrupt the decoding of the first detected error and therefore to reject the bits that can contribute to the propagation of errors.

We suppose that we have a set:

$$C = \{c_1(N_{c_1}, K_{c_1}), c_2(N_{c_2}, K_{c_2}), \dots, c_L(N_{c_L}, K_{c_L})\} \quad (5)$$

Of errors correction codes. The compressed bit frame is formatted into packets of variable length. Each packet of length  $K_{cl}$  bits is encoded by a code  $c_L \in C$  to generate a coded packet of length  $N_{cl}$  bits. We introduce, for each  $c_L \in C$ , the following ratios, expressed in bits per symbol of the source:

$$r_m(c_l) = \frac{K_{cl}}{H_s}(bpp) \text{ et } r_c(c_l) = \frac{N_{cl}}{H_s}(bpp) \quad (6)$$

At the receiver, the decoding is stopped at the first detected erroneous packet, since the following packets are generally unable to improve the quality of the decoded picture. We will assume, in what follows, that the probability of not detecting an erroneous packet is zero (perfect detection). On the other hand, we note  $P_e(c_l)$  the probability that a packet coded by the error correction code  $c_l$  and transmitted on the channel in question, is incorrect after decoding.

Given a global transmission rate  $R_T$  (source coding + channel coding), the optimization objective of the unequal protection consists in determining an optimal policy (or strategy) for allocating codes to the different data packets, according to a

given performance measurement criterion. Note that a code allocation policy is defined as a sequence of codes

$$\pi = \{c_\pi^1(N_{c_\pi^1}, K_{c_\pi^1}), c_\pi^2(N_{c_\pi^2}, K_{c_\pi^2}), \dots, c_\pi^{M_\pi}(N_{c_\pi^{M_\pi}}, K_{c_\pi^{M_\pi}})\}$$

Applying the error correction code  $c_\pi^i \in C$  to the  $i^{th}$  packet of data, taken of length equal to bits,  $i = 1, 2, 3, \dots, M_\pi$ ;  $M_\pi$  being the number of packets to be transmitted using the  $\pi$  policy; it is also the index of the last transmitted packet. The overall transmission rate relating to the policy  $\pi$  is, then, given by:

$$R_{T\pi} = \sum_{i=1}^{M_\pi} r_c(c_\pi^i)(bpp) \quad (7)$$

The constraint flow can therefore be expressed by inequality:

$$R_{T\pi} \leq R_T$$

**OPTIMIZATION CRITERIA**

Several performance measures can be adopted to characterize the performance of a given code allocation policy, and thus serve as criteria to be optimized.

Among these distortion measurements between the original image and the decoded image, there are:

- . Quadratic Mean Error (MSE).
- . The PSNR.

The bits number correctly decoded and used for the image reconstruction, or else the Useful Reconstruction Rate, which will be designated by DUR (criterion valid in the case of a nested source coding).

We give:

$$r_{\pi,i} = \sum_{j=1}^i r_m(c_\pi^j)(bpp) \quad (8)$$

Describing the useful bit rate of image reconstruction when the  $(i + 1)^{th}$  packet is detected false.

We will, in what follows, give, for a policy:

$$\pi = \{c_\pi^1(N_{c_\pi^1}, K_{c_\pi^1}), c_\pi^2(N_{c_\pi^2}, K_{c_\pi^2}), \dots, c_\pi^{M_\pi}(N_{c_\pi^{M_\pi}}, K_{c_\pi^{M_\pi}})\}$$

Given the respective means (mathematical expectations) of the MSE, noted  $\overline{MQE\pi}$ , of the PSNR, noted  $\overline{PSNR\pi}$  and the Useful Rate of Reconstruction, noted  $\overline{DUR\pi}$ :

$$\overline{MSE\pi} = MSE(r_{\pi,0})P_e(c_\pi^1, P_b) + \sum_{i=2}^{M_\pi+1} MSE(r_{\pi,i-1})P_e(c_\pi^i, P_b) \prod_{j=1}^{i-1} [1 - P_e(c_\pi^j, P_b)] \quad (9)$$

$$\overline{PSNR\pi} = PSNR(r_{\pi,0})P_e(c_\pi^1, P_b) + \sum_{i=2}^{M_\pi+1} PSNR(r_{\pi,i-1})P_e(c_\pi^i, P_b) \prod_{j=1}^{i-1} [1 - P_e(c_\pi^j, P_b)] \quad (10)$$

$$\overline{DUR\pi} = r_{\pi,0}P_e(c_\pi^1, P_b) + \sum_{i=2}^{M_\pi+1} r_{\pi,i-1}P_e(c_\pi^i, P_b) \prod_{j=1}^{i-1} [1 - P_e(c_\pi^j, P_b)] \quad (11)$$

MSE (r) designates the function representing (in the absence of noise) the Mean Square Error (MSE) as a function of the rate r (in bpp) for the encoder of source used and in the case of the image to be transmitted.

$$PSNR(r) = 10 \log_{10} \left( \frac{255^2}{MSE(r)} \right) dB \quad (12)$$

$P_e(c_\pi^i, P_b)$  is the probability of an error at least at the  $i$ th packet (using the code  $c_\pi^i$ ) as a function of the probability  $P_b$  (probability of error per bit).

In the case of equal error protection EEP:

$c_\pi^i = c_\pi$  is constant. So it can be written:

$$\overline{MSE}_\pi = P_e(c_\pi, P_b) \sum_{i=1}^{M_\pi+1} MSE(r_{\pi,i-1}) [1 - P_e(c_\pi, P_b)]^{i-1} \quad (13)$$

Therefore, it is necessary to determine the code  $c_\pi$  (channel coding) which minimizes the distortion by ensuring a maximum information transmission with the minimum of error.

$R_{c_\pi} = K_{c_\pi}/N_{c_\pi}$  is characterized by the probabilities:

$P_b$ : Probability of error per bit characterizing the channel.

And  $P_e(c_\pi, P_b)$ : Probability of error per packet, for the code  $c_\pi$  and for the probability  $P_b$ . One notes that a packet is considered erroneous if one detects at least one error in the packet.

These three performance measures lead to the following three optimization problems:

Problem I: minimization of the average MSE:

$$\min_{\pi} \overline{MSE}_\pi \text{ under the constraint } R_{T\pi} \leq R_T$$

Problem II: maximization of average PSNR

$$\max_{\pi} \overline{PSNR}_\pi \text{ under the constraint } R_{T\pi} \leq R_T$$

Problem III: maximizing the useful average of reconstruction:

$$\max_{\pi} \overline{DUR}_\pi \text{ under the constraint } R_{T\pi} \leq R_T$$

It is noted that the performance measures used in Problems I and II (MSE and PSNR) are more representative of the quality of the reconstructed image than that used in Problem III. Nevertheless, the advantage of the latter is that it does not use functions characterizing the performance of the source code in the case of the image in question (MSE (r) or PSNR (r) functions). Therefore, it is not necessary to transmit to the receiver the code allocation policy that has been encoder level. We will, in the following, consider the problem 1.

### DETERMINATION OF OPTIMAL SOLUTIONS

In our case it is assumed that the length of the packets at the output of the channel coder is fixed:

$N_{c_\pi^i} = N_\pi = \text{constant}$ . But the data packets to be coded are of variable length so the number of redundancy bits in each packet is variable. Therefore, to specify the number of source bits  $K_{c_\pi^i}$  is equivalent to specifying the number of redundancy

bits  $N_\pi - K_{c_\pi^i}$  in the  $i$ th packet.

In the case of the EEP protection, one must find the code  $c_\pi$  of yield  $R_{c_\pi} = K_{c_\pi}/N_{c_\pi}$  which minimizes the expression (13) by ensuring a transmission of maximum information with the minimum of error.

But in the case of the UEP protection, it is necessary to determine for each packet the efficiency  $R_{c_\pi^i} = K_{c_\pi^i}/N_\pi$  of the encoder correctors  $c_\pi^i(N_\pi, K_{c_\pi^i})$  which minimizes the expression (9) by ensuring a maximum information transmission with the minimum of error.

The code  $c_\pi^i(N_\pi, K_{c_\pi^i})$  is chosen from L error correcting codes:

$$C = \{c_1(N_\pi, K_{c_1}), c_2(N_\pi, K_{c_2}), \dots, c_L(N_\pi, K_{c_L})\}$$

So we have  $M^L$  possible combination of Code Rates, with P is the number of turbochargers different yield and M is the number of packets to transmit.

In our simulation, we adopted a simple optimization method, consists in finding in the EEP protection for the set of packets (Table 1) With  $\mathcal{E} = 10^{-2}$ .

**Table 1:** Optimization (Rs) Code Steps By The Pattern Search (Ps) Of Eep Protection

|              |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
|--------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>steps</b> | <p><i>Step 1: Select Performance R.</i></p> <p><i>Step 2: Extract the RS (M, t) code input parameters according to the R output.</i></p> <p><i>Step 3: Apply the RS code (M, t) parameters on the set of packets.</i></p> <p><i>Step 4: Inject the Channel noise on the set of packets.</i></p> <p><i>Step 5: Correct the erroneous bits.</i></p> <p><i>Step 6: If (MSE of the reconstructed image - MSE of the received image) <math>\leq \mathcal{E}</math>. with min redundancy bits</i></p> <p><i>End</i></p> <p><i>Step 7: If not go to step 1.</i></p> |
|--------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

For UEP protection by protecting more important packets for image reconstruction. (Table 2) With  $\mathcal{E} = 10^{-2}$

This algorithm is more efficient than those used in the literature. And its main advantage is its speed and rapid convergence.

**Table 2:** Optimization (RS) Code Steps by the UEP Protection Pattern Search (PS)

|              |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
|--------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>steps</b> | <p><i>Step 1: Select the <math>R_i</math> Code Rates.</i></p> <p><i>Step 2: Extract the encoder input parameters RS (<math>M_i, t_i</math>) for each output <math>R_i</math>.</i></p> <p><i>Step 3: Apply RS encoder parameters (<math>M_i, t_i</math>) on each packet.</i></p> <p><i>Step 4: Inject the Channel noise on each packet to transmit.</i></p> <p><i>Step 5: Correct the erroneous bits.</i></p> <p><i>Step 6: Group the packages</i></p> <p><i>Step 7: rebuild the received image.</i></p> <p><i>Step 8: If (<math>MSE</math> of the reconstructed image - <math>MSE</math> of the received image) <math>\leq \epsilon</math>. with min redundancy bits</i></p> <p><i>End</i></p> <p><i>Step 9: If not go to step 1.</i></p> |
|--------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

**A. Application to solomon reed**

The flow allocation optimization method presented above is applied to the image transmission system of Fig. 8. The Lena image is taken as a test image. The transmission is done on a symmetrical binary bit error rate channel varying from 10-3, 10-2 and 10-1. For each BER of the channel, optimization is performed for a rate value: CR = 0.25 bpp.

The data delivered by the SPIHT encoder is partitioned into consecutive blocks of size ( $R_i-16$ ) bits each. It is assumed that the channel coding strategy is done in two steps: an error-detector coding (CRC) followed by an error-correcting coding (reed solomon code: (RS)). The role of error detection is to interrupt the decoding of the first detected error and therefore to reject the bits that can contribute to the propagation of errors. At the receiver, the decoding is stopped at the first detected erroneous packet, since the following packets are generally unable to improve the quality of the decoded picture. The CRC encoder adds 16 redundancy bits to each block.

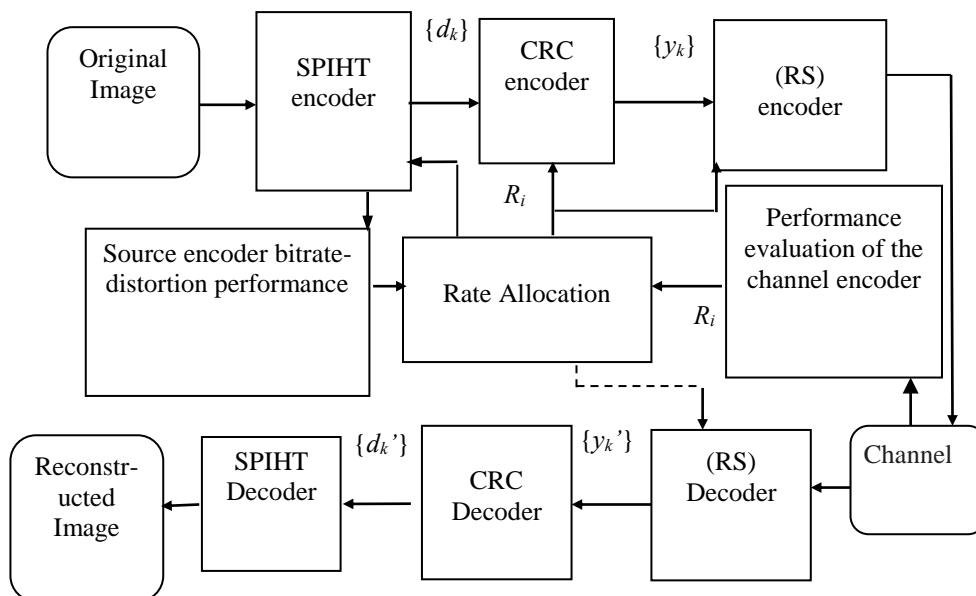
The resulting data is transmitted on a channel without memory. At the receiver, the RS is decoded. The use of these codes makes it possible to have very high coding efficiencies giving rise to a better spectral efficiency of the system. However, for the choice of coding efficiencies, it is often necessary to use genetics for the automatic selection. For this, we consider a set of 08 different yield codes: {0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9}. These codes are derived from an RS. All results are based on a packet length of 16386 bits at the output of the channel encoder.

For each BER of the channel, the optimal code allocation policies according to the minimization criteria of the average MSE (Problem I), are determined by the source coder considered: SPIHT. This problem has been chosen for its effectiveness in optimizing the proposed system.

For BER = 0.001

PSNRrec: reconstructed PSNR

PSNRreç: PSNR received



**Figure 8:** Applied to the image transmission system

**Table 1:** versus BER of a BSC channel for both Lena and Goldhill images (512 × 512) For BER = 0.001.

| Total CR (0.25 bpp)                  | BER of channel 0.001 |            |     |     |     |         |
|--------------------------------------|----------------------|------------|-----|-----|-----|---------|
|                                      | 04 packets           |            |     |     |     |         |
|                                      | PSNRrec              | Code Rates |     |     |     | PSNRreç |
| lena image                           | 34.1186              | 0.8        | 0.9 | 0.9 | 0.9 | 34.1062 |
| Godhill image                        | 30.5609              | 0.7        | 0.7 | 0.8 | 0.8 | 30.5483 |
| Redundancy bits<br>For image lena    | 5357                 |            |     |     |     |         |
| Redundancy bits<br>For image Godhill | 13597                |            |     |     |     |         |

**Table 3:** versus BER of a BSC channel for both Lena and Goldhill images (512 × 512) For BER = 0.01.

| Total CR (0.25 bpp)                  | BER of channel 0.01 |            |     |     |     |         |
|--------------------------------------|---------------------|------------|-----|-----|-----|---------|
|                                      | 04 paquets          |            |     |     |     |         |
|                                      | PSNRrec             | Code Rates |     |     |     | PSNRreç |
| lena image                           | 34.1186             | 0.3        | 0.4 | 0.5 | 0.5 | 32.4739 |
| Godhill image                        | 30.5609             | 0.3        | 0.6 | 0.6 | 0.7 | 29.6433 |
| Redundancy bits<br>For image lena    | 29674               |            |     |     |     |         |
| Redundancy bits<br>For image Godhill | 28694               |            |     |     |     |         |

**Table 4:** versus BER of a BSC channel for both Lena and Goldhill images (512 × 512) For BER = 0.1.

| Total CR (0.25 bpp)                  | BER of channel 0.1 |            |     |     |     |         |
|--------------------------------------|--------------------|------------|-----|-----|-----|---------|
|                                      | 04 paquets         |            |     |     |     |         |
|                                      | PSNRrec            | Code Rates |     |     |     | PSNRreç |
| lena image                           | 34.1186            | 0.2        | 0.2 | 0.2 | 0.3 | 27.8089 |
| Godhill image                        | 30.5609            | 0.2        | 0.2 | 0.2 | 0.2 | 26.6165 |
| Redundancy bits<br>For image lena    | 50352              |            |     |     |     |         |
| Redundancy bits<br>For image Godhill | 52447              |            |     |     |     |         |

We have shown in Table 6 the respective variations of the optimal PSNR.

The coding system performance introduced by [15], [16] and [17] is presented.



**Table 5:** PSNR versus BER of a BSC channel for the Lena  $512 \times 512$  image using the SPIHT encoder

| Total CR (0.25 bpp)                    | BER of channel 0.01 |       |
|----------------------------------------|---------------------|-------|
|                                        | Code Rate           | PSNR  |
| Sachs et al.<br>(mother rate 1/2) [15] | 0.30                | 27.90 |
| Thomos et al. "TCS-UEP" [16]           | 0.33                | 28.64 |
| Thomos et al. "TCSD-UEP" [16]          | 0.33                | 28.73 |
| Usama Sayed et Safwat M "UEP" [17]     | 0.29                | 30.32 |
| Système proposé                        | 0.4                 | 32.47 |

Tables.3. 4. 5 and.6 show, in fact, that the proposed algorithm often allows to find an optimal solution of the problem I.

It is obvious that the performances obtained by applying the UEP protection are better than those obtained by applying the EEP protection.

## CONCLUSION

In this paper, we considered the rate allocation optimization the between a nested source encoder and a channel encoder, for a transmission of still images through a BSC channel. We retained the reed solomon (RS) code for data protection because they offer the best performance, in error correction terms, on a binary output channel. We have proposed the unequal protection optimization by different RSs, of the progressive bit stream delivered by the source code. An error detection provided by the CRC codec makes it possible to stop the decoding at the first detected erroneous block and to reconstruct the image from the blocks that are supposed to be correct.

We considered a transmission on a BSC channel two optimization criteria were presented: Quadratic Mean Error (MSE), peak signal-to-noise ratio (PSNR). The optimization method developed will be applied to the SPIHT encoder for compression of the source image. Our simulations have shown that, in the context of coding and transmission considered, the optimal performances obtained with the SPIHT coder are very close. We also noted that the criterion of MSE optimization is the most relevant criterion, as it ensures a better minimum quality of the decoded image at the expense of a slight degradation of the decoded PSNR in the first time with errors absence. Finally, the gain provided by the application of unequal protection (compared to uniform protection) depends both on the source encoder used and the error correction codes considered.

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