

# Satellite Image Resolution Enhancement Using Non-Decimated Wavelet Transform and Gaussian Mixture Model

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## Abstract

High resolution satellite images are of significant importance in many fields of research and its enhancement is an active research area. Among various techniques used for image resolution enhancement Wavelet based techniques have been found to be very efficient. Discrete Wavelet Transform (DWT) is mostly used in image decomposition stage but suffers from shift variance. In this work Non-Decimated Wavelet Transform (NDWT) which is shift invariant is investigated. Instead of Bicubic interpolation Gaussian Mixture Model (GMM) which is a parametric probability density function represented as a weighted sum of Gaussian component densities is used instead of weighted sum of neighborhood pixels used by bicubic and bilinear interpolations. The proposed technique showed improved Peak Signal to Noise Ratio (PSNR) and Quality Index.

**Keywords:** Bicubic Interpolation; Discrete Wavelet Transform (DWT); Gaussian Mixture Model (GMM); Non-Decimated Wavelet Transform (NDWT); Peak Signal-to-Noise Ratio (PSNR); Quality Index (QI);

## Introduction

Satellite images are used in many applications such as geoscience studies, weather forecasting, astronomy and geographical information systems [1]. However, high resolution satellite images are essential for better results and thus image resolution enhancement plays a crucial role. Popular techniques used in literature include nearest neighbour interpolation, bilinear interpolation and bicubic interpolation [2]. Bicubic interpolation is widely compared to the other two techniques and it produces noticeably sharper images [3]. When applying interpolation methods, the high frequency components may be eliminated because of the smoothing effects created during interpolation. It is imperative that pixel values around the edges be preserved to improve the

resolution of the image. Wavelets play a vital role in image resolution enhancement techniques to preserve the edges. Discrete Wavelet Transform (DWT) is used in image decomposition stage and bicubic interpolation is used in interpolation stage in many of the wavelet based image resolution enhancement methods [4][5]. DWT decomposes the image into four sub band images defined as Low-Low (LL), Low-High (LH), High-Low (HL), and High-High (HH). The frequency components of these sub bands cover the full frequency spectrum of the original image. Theoretically, a filter bank should be operated on the image in order to generate different sub band frequency images. Edges identified in lower frequency sub bands are used to prepare the model for estimating edges in higher frequency sub-bands, and only the coefficients with significant values are estimated as the evolution of the wavelet coefficients. Filter bank of DWT is shown in figure1 [6].

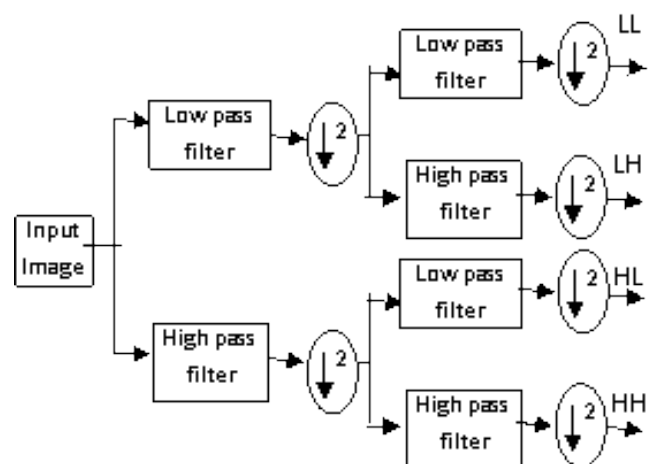


Figure 1. Filter Bank of DWT

Hasan et al [4] proposed a resolution enhancement technique based on the image decomposition using DWT and coefficients are interpolated using bicubic interpolation. When tested on satellite benchmark images the quantitative and visual results showed that their proposed technique was superior to the conventional image resolution enhancement techniques. Battulla et al., [7], Mohan, et al., [8] and Karunakar et al., [9] also proposed DWT decomposition and interpolation of high frequency components. Salehi and Nasab presented image resolution improvement method based on the complex wavelet transform and feed forward Neural Networks (NN) [10]. The wavelet sub bands of high resolution images are constructed by using the NN using the low resolution sub bands. Dual complex tree properties such as approximate shift variance, directional selectivity and substantial reduced aliasing were used to get detailed representation of the local structures in the interpolated images.

Zhang [11] proposed edge-guided nonlinear interpolation method by using a directional filtering and data fusion. To interpolate a pixel, two observation sets are created in two orthogonal directions, and each set produces an estimate of the pixel value. These estimated sets were modeled as different noisy measurements in missing pixels and fused by the Linear Minimum Mean Square-Error Estimation (LMMSE) technique using the statistics. Experiments show that the proposed interpolation method preserved sharpness of edges and reduced the ringing artifacts. Huayong et al., [12] proposed a novel method for single image super-resolution. From the input low-resolution images, a pyramid pair was constructed by using the ground truth pyramid and the interpolated pyramid. The relationship between pixel value in ground truth pyramid and its corresponding 8-neighborhood vector in interpolated pyramid was found by using GMM. All the pixel values of the high-resolution image were estimated by using the corresponding 8-neighborhood vector through the trained GMM. Taquet et al., [13] proposed an interpolation scheme based on Gaussian mixture simplification and demonstrated the advantages over a heuristic approach by means of the spatial normalization and tractography results by using Diffusion Tensor Imaging. The results were compared with the conventional bi linear and bi cubic interpolation methods and it was demonstrated that their proposed method was better as it accurately reconstructed the edges and textures at low cost. Hou et al [14] proposed two synthetic aperture radar complex image compression schemes based on Directional Lifting Wavelet Transform Image Quality (DLWT\_IQ) and DLWT\_ Fast Fourier Transform (DLWT\_FFT). The real parts and imaginary parts of the images are encoded by DLWT\_IQ and the real images are converted by FFT is encoded by DLWT\_FFT.

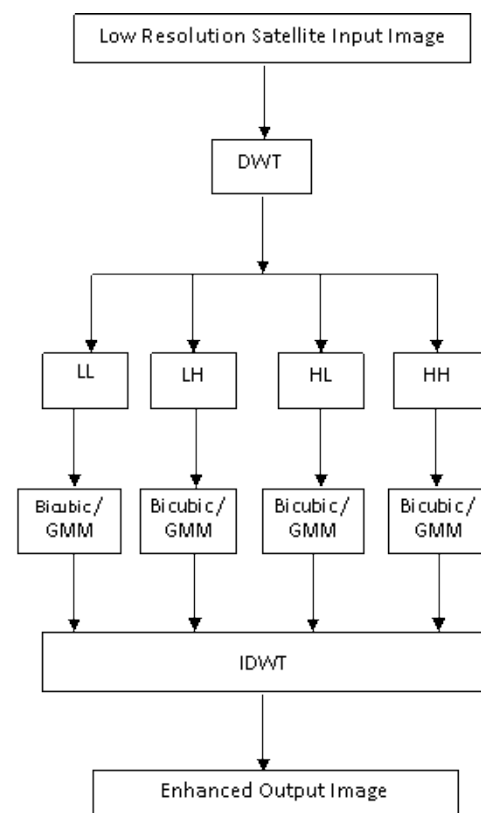
DWT suffers from shift variance and bicubic interpolation gives rise to blurred edges. To overcome this, a new image resolution enhancement technique Non-Decimated Wavelet Transform (NDWT) image decomposition and Gaussian Mixture Model (GMM) interpolation is proposed in this paper. Each sub band within the NDWT decomposition has the same number of coefficients as the number of samples in the original signal, thus leading to complete representation and completely shift invariant. GMM is a flexible, semi-

parametric model, yet simple model which makes efficient estimations.

The flow chart for Satellite Image Resolution Enhancement using DWT and interpolation using Bicubic and Gaussian Mixture Model (GMM) is shown in figure2. Here DWT is used to decompose an input image into Low Low (LL), Low High (LH), High Low (HL) and High High (HH) sub bands. These sub bands are interpolated using Bicubic interpolation technique, followed by combining all these images to generate a new high-resolution image by using inverse DWT. Results of this technique are compared with proposed technique.

When applying interpolation methods, the high frequency components may be lost as the coefficients of DWT are inherently interposable. But Down sampling in each of the DWT sub bands will cause loss of information in the respective sub bands. DWT is a non redundant transform and artifacts such as ringing are introduced when transform coefficients are modified and this can be eliminated by using NDWT.

This paper is organized as follows: Section2 gives an overview on the bicubic interpolation, Section 3 introduces the proposed NDWT and GMM interpolation technique and Section 4 discusses the visual and quantitative results of the proposed techniques. The results of the proposed method are compared with other conventional techniques. Both quantitative and visual results show the superiority of the proposed technique. Conclusions are given in the final section.



**Figure 2. Block diagram of Image decomposition using DWT and Bi-cubic / GMM interpolation Satellite Image Resolution Enhancement Technique.**

## 2. Bicubic Interpolation

Interpolation is a commonly used method for resolution enhancement. In linear interpolation method, mean value of neighbouring pixels is used to interpolate at each pixel, but it may create blurred edges and smoothed details. In bilinear interpolation, new pixel value is computed by weighted average of four surrounding pixels. This will be useful for image compression instead of image resolution enhancement to reduce the redundancy. Many non-linear interpolation (bicubic) methods are more powerful than linear methods (bilinear) [7]. However, if the raw image has more lower-frequency information, it is better to use the bilinear interpolation rather than bicubic interpolation. In bicubic interpolation, interpolated point is filled with sixteen closest pixel's weighted average [7]. The bicubic convolution interpolation kernel is:

Where  $a$  is generally taken as 0.5 to 0.75

## 3 Proposed Technique

In this section NDWT and GMM is discussed followed by the proposed technique.

### 3.1 Non Decimated Wavelet Transform

The Discrete Wavelet Transform is not a time invariant transform. The way to restore the translation invariance is to average some slightly different DWT, called Non-decimated or un-decimated DWT (NDWT or UDWT). It does so by suppressing the down-sampling step of the decimated algorithm and instead of up-sampling the coefficients are interpolated by inserting zeros between the filter coefficients. As with the decimated algorithm, the filters are applied first to the rows and then to the columns. In this case, however, although the four images produced (one approximation and three detail images) are at half the resolution of the original and they are the same size as the original image. The approximation images from the non-decimated algorithm are therefore represented as levels in a parallelepiped, with the spatial resolution becoming coarser at each higher level and the size remaining the same. The 2D NDWT is based on the idea of no decimation. It applies the DWT and omits both down-sampling in the forward and up-sampling in the inverse transform. More precisely, it applies the transform at each point of the image and saves the detail coefficients and uses the low frequency information at each level [15].

The Non Decimated Wavelet Transform 'W' using the filter bank  $h, g$  representing high pass and low pass respectively of a 1-D signal  $C_0$  leads to a set  $W = \{w_i, \dots, w_j, c_j\}$  where  $w_j$  are the wavelet coefficients at scale  $j$  and  $c_j$  are the coefficients at the coarsest resolution. The passage from one resolution to the next one is obtained using the "à trous" algorithm.

$$c_{j+1}[l] = (\bar{h}^{(j)} * c_j)[l] = \sum_k h[k] c_j[l + 2^j k] \quad (2)$$

$$w_{j+1}[l] = (\bar{g}^{(j)} * c_j)[l] = \sum_k g[k] c_j[l + 2^j k] \quad (3)$$

Here  $h^{(j)}[l] = h[l]$  if  $l/2^j$  is an integer and zero.

For example

$$h^{(0)} = (\dots, h[-2], 0, h[-1], 0, h[0], 0, h[1], 0, h[2], 0, \dots)$$

The reconstruction is done by,

$$c_j[l] = \frac{1}{2} \left[ (\tilde{h}^{(j)} * c_{j+1}[l]) + (\tilde{g}^{(j)} * w_{j+1}[l]) \right] \quad (4)$$

The filter bank  $(h, g)$  and  $(\tilde{h}, \tilde{g})$  has to check the reconstruction condition given by,

$$H(z^{-1})\tilde{H}(z) + G(z^{-1})\tilde{G}(z) = 1 \quad (5)$$

This provides us with a higher degree of freedom when designing the synthesis prototype filter bank. The à trous algorithm can be extended to 2D by

$$c_{j+1}[k, l] = (\bar{h}^{(j)} \bar{h}^{(j)} * c_j)[k, l] \quad (6)$$

$$w_{j+1}^1[k, l] = (\bar{g}^{(j)} \bar{h}^{(j)} * c_j)[k, l] \quad (7)$$

$$w_{j+1}^2[k, l] = (\bar{h}^{(j)} \bar{g}^{(j)} * c_j)[k, l] \quad (8)$$

$$w_{j+1}^3[k, l] = (\bar{g}^{(j)} \bar{g}^{(j)} * c_j)[k, l] \quad (9)$$

Where  $hg * c$  is the convolution of  $c$  by the separable filter  $hg$  (i. e., convolution first along the columns by  $h$  and then convolution along the rows by  $g$ ). At each scale, we have three wavelet images  $w^1, w^2, w^3$  and each has the same size as the original image [16]. For a real discrete-time filter whose impulse response is  $h[n]$ ,  $\bar{h}[n] = h[-n]$ ,  $n \in \mathbb{Z}$  is its time-reversed version. For the octave band non sub sampled wavelet representation, analysis and synthesis filters are denoted by  $(h, g)$  and  $(\tilde{h}, \tilde{g})$  respectively will be used for the Fourier transform of square-integral signals.

### 3.2 Gaussian Mixture Model

Edge structures preservation is a challenging task during the interpolation of images while reconstructing a high-resolution image using low-resolution counterpart. In this proposed technique, input image is decomposed with NDWT and coefficients are interpolated with the highest probability of covariance matrix  $\Sigma_i$  and mean  $\mu_i$  rather than weighted average of sixteen neighbour pixels used in bicubic interpolation. So it gives sharper edges and better PSNR and QI than bicubic interpolation.

A GMM is a parametric probability density function represented as a weighted sum of Gaussian component densities. GMMs are commonly used as a parametric model of the probability distribution of continuous measurements. The complete Gaussian mixture model is parameterized by the mean vectors, covariance matrices and mixture weights from all component densities. The covariance matrices can be full rank or constrained to be diagonal. Additionally, parameters can be shared, or tied, among the Gaussian components, such as having a common covariance matrix for all components. The choice of model configuration including number of components, full or diagonal covariance matrices, and parameter tying are determined by the amount of data available for estimating the GMM parameters and how the GMM is used. A Gaussian mixture model is a weighted sum of  $M$  component Gaussian densities [17] is represented by equation (10).

$$p(x|\lambda) = \sum_{i=1}^M w_i g(x|\mu_i, \Sigma_i) \quad (10)$$

Where  $x$  is a D-dimensional continuous-valued data is vector and depends on the number of dimensions in the data.  $\lambda$  represents the parameterized model of the Gaussian mixture and made up of mean vectors, covariance matrices and mixture weights  $\{\mu_i, w_i, \Sigma_i\}$ .

In the case of gray scale image  $D=2$ .  $w_i, i = 1, \dots, M$ , mixture weights.

$g(x|\mu_i, \Sigma_i), i = 1, \dots, M$ , Gaussian densities component. Density component is a D-variate Gaussian function consisting of D dimensions given as,

$$g(x|\mu_i, \Sigma_i) = \frac{1}{(2\pi)^{D/2} |\Sigma_i|^{1/2}} \exp\left\{-\frac{1}{2}(x-\mu_i)' \Sigma_i^{-1} (x-\mu_i)\right\}$$

Where  $\mu_i$ -mean vector and it is given as  $\mu_i = \frac{\sum_{i=1}^n x_i}{n}$  and  $\Sigma_i$  is a covariance matrix and it is given as

$$\Sigma_i = \frac{\sum_{i=1}^n (x_i - \bar{x})(x_i - \bar{x})'}{n - 1}$$

In probability theory, covariance is a measure of how much two random variables change together. The mixture weights

satisfy the constraint  $\sum_{i=1}^M w_i = 1$ . Thus, the Gaussian mixture model is represented by the mean vectors, covariance matrices and mixture weights of all component densities. The problem is formulated to the prediction of wavelet coefficients of an image and use the inverse wavelet transform resulting in increased resolution. Training of the mixture model is achieved using Expectation Maximization (EM) algorithm. For a given wavelet coefficient 'c' that is governed by a group of parameters  $\theta$  the density function is given by  $p(x/\theta)$ . Let N be the size of the coefficients and assuming each coefficient is independent and identically distributed with distribution p, the resulting likelihood can be given by

$$p(C/\theta) = \prod_{i=1}^N p(c_i/\theta) = \ell(\theta/C)$$

The function  $\ell(\theta/C)$  is called the likelihood of the given input wavelet coefficients.

Using EM algorithm it is possible to find additional values. Assuming the coefficients C is generated by some distribution, it can be stated C is the incomplete and assuming a complete data  $E = (C, D)$  exists such that the joint density function is given by

$$p(E/\theta) = p(c, d/\theta) = p(d/c, \theta) p(c/\theta)$$

The EM algorithm finds the expected value and is given by  $O(\theta, \theta^{(i-1)c}) = E \log p(C, D|\theta) | C, \theta^{(i-1)}$

Where  $\theta^{(i-1)}$  are the current parameter estimates used to evaluate expectation. The proposed technique is shown as in figure 3

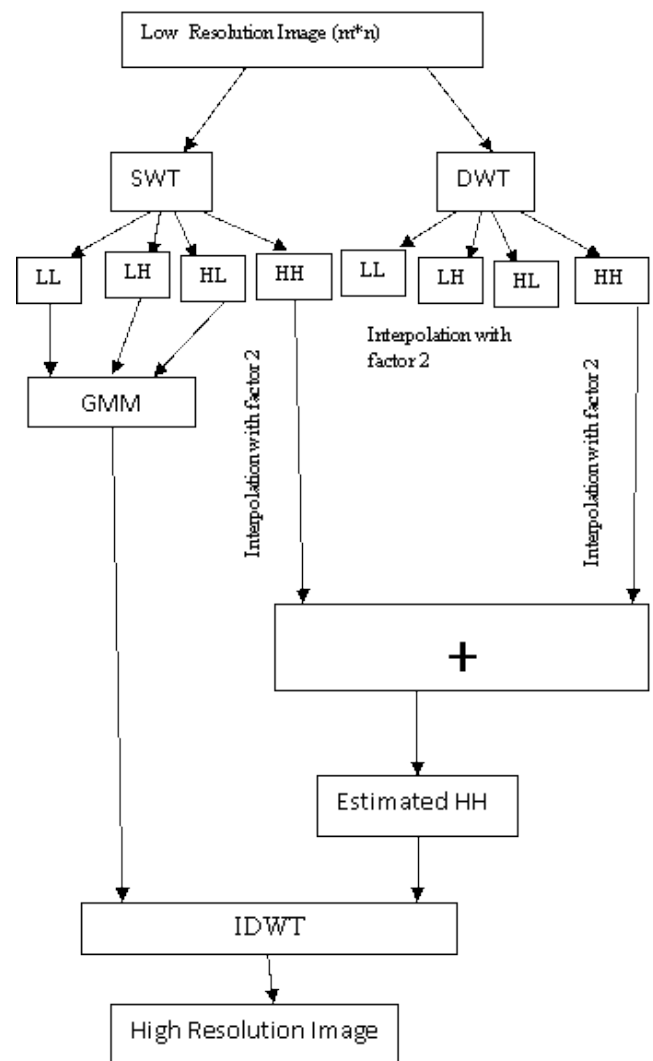
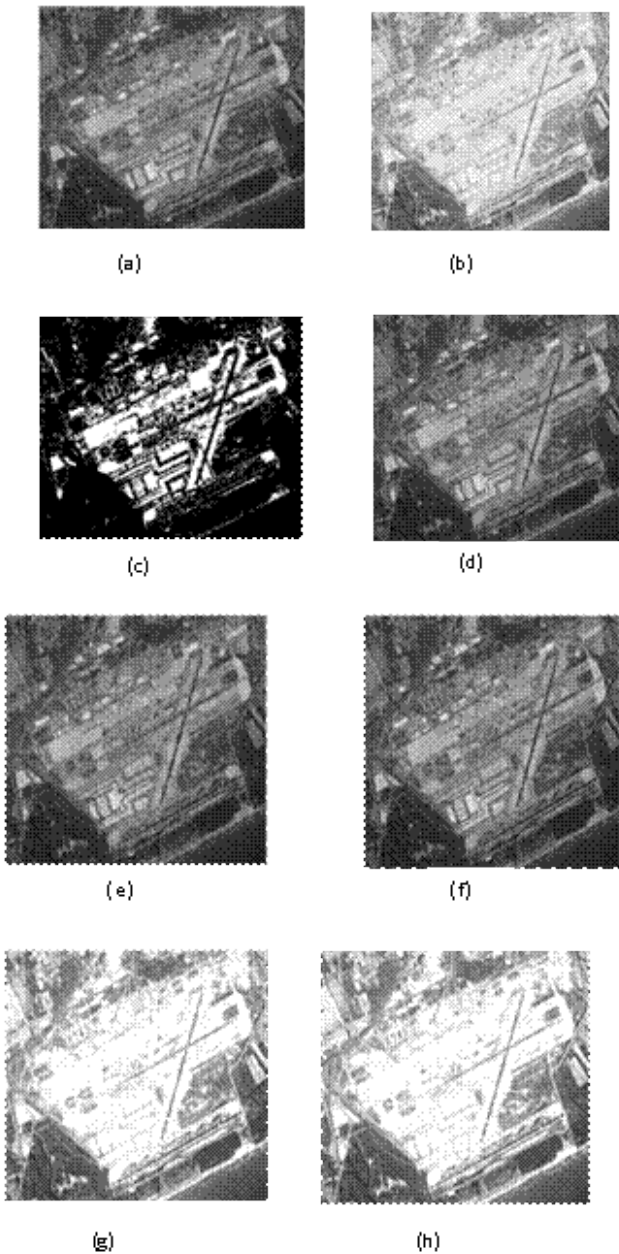


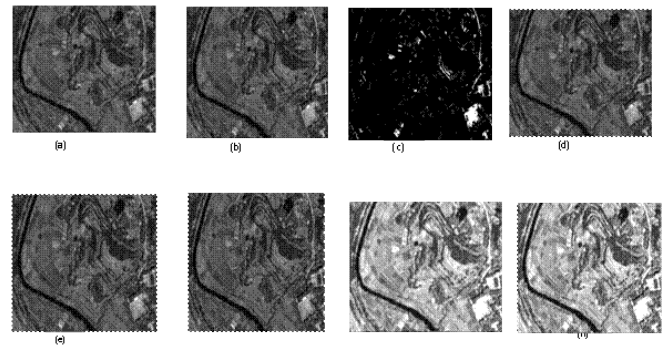
Figure 3: Proposed architecture

#### 4. Experimental Results

In order to show the improvement in the resolution of satellite images of the proposed method over the conventional and state-of-art image resolution enhancement techniques, two satellite images with different features are used for comparison. Fig. 4 and Figure. 5 show that high resolution images using the proposed techniques in (f) and (h) are much sharper than the original low-resolution images in (a), bilinear interpolation in (b), bicubic interpolation in (c) wavelet zero padding in (d), DWT based image decomposition and bicubic interpolated images in (e). The proposed technique is evaluated in terms of Peak Signal to Noise Ratio (PSNR), and Quality Index (QI) and compared with other techniques. It is clear that the proposed DWT-GMM and NDWT-GMM techniques outperform than bilinear interpolation, bicubic interpolation, wavelet zero padding and DWT based image decomposition and bicubic interpolated techniques.



**Figure 4. Satellite Image of US-Topo (a) Low Resolution Input Image, Resolution Enhanced Images using (b) Bilinear Interpolation, (c) Bicubic Interpolation, (d) Wavelet Zero Padding, (e) DWT based Image decomposition and bicubic interpolated image. (f) DWT based Image decomposition and GMM interpolated image, (g) NDWT based decomposition and bicubic interpolated image. (h) Proposed Technique (NDWT based decomposition and GMM interpolated) image.**



**Figure 5. Satellite image of Washington-DC (a) Low resolution input image, Resolution enhanced images using (b) Bilinear Interpolation, (c) Bicubic Interpolation, (d) Wavelet Zero Padding, (e) DWT based decomposition and bi-cubic interpolated image. (f) DWT based decomposition and GMM interpolated image, (g) NDWT based decomposition and bi-cubic interpolated image. (h) Proposed Technique (NDWT based decomposition and GMM interpolated image).**

**The PSNR is calculated as follows:**

PSNR is the ratio of the maximum possible power of a signal and the power of noise and is expressed in logarithmic decibel scale 10.

$$PSNR = 10 \log_{10} \frac{255^2}{MSE} \tag{11}$$

$$MSE = \frac{\sum_{i=1}^X \sum_{j=1}^Y (a_{i,j} - b_{i,j})^2}{xy} \tag{12}$$

MSE is a Mean Square Error, where the terms  $a_{i,j}$  and  $b_{i,j}$  represent the pixel values from actual and the interpolated images respectively and. the values X and Y define the height and width of an image respectively.

And the Quality Index is calculated as below:

Let  $x = \{x_i | i = 1, 2, \dots, N\}$  and  $y = \{y_i | i = 1, 2, \dots, N\}$  be the original and the test image signals respectively. The proposed quality index is defined as

$$Q = \frac{4\sigma_{xy} \bar{x} \bar{y}}{(\sigma_x^2 + \sigma_y^2) [(\bar{x})^2 + (\bar{y})^2]} \tag{13}$$

Where  $\bar{x} = \frac{1}{N} \sum_{i=1}^N x_i$ ,  $\bar{y} = \frac{1}{N} \sum_{i=1}^N y_i$

$$\sigma_x^2 = \frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2, \quad \sigma_y^2 = \frac{1}{N-1} \sum_{i=1}^N (y_i - \bar{y})^2$$

$$\sigma_{xy} = \frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})(y_i - \bar{y})$$

Figure 6 and 7 show the PSNR for the Satellite Image of US-TOPO and Satellite image of Washington-DC respectively. The PSNR of the proposed technique is 6. 2544dB and 4. 66 higher than the PSNR of DWT and bicubic interpolation technique respectively.

The Q index of proposed technique is 1. 9193 and 1. 9853 dB higher than the Q index obtained by using DWT and bicubic interpolation techniques for image1 and image2 respectively.

Results indicate the superiority of the proposed technique over the conventional and image resolution enhancement techniques.

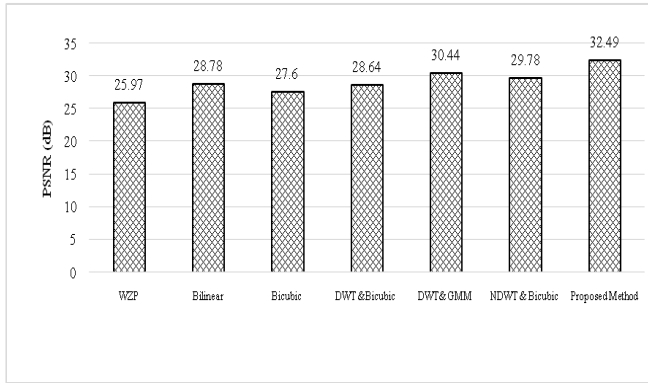


Figure 6 PSNR (Decibels) results for resolution enhancement for the proposed technique compared with conventional and some state-of-art techniques.

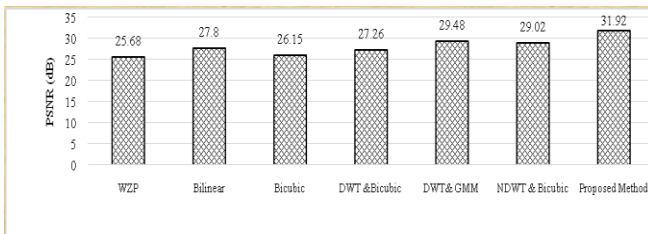


Figure 7 PSNR for Satellite Image of Washington-DC.

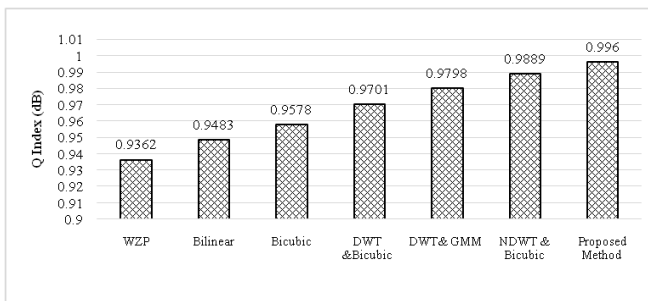


Figure 8 Q index for Satellite Image of US-TOPO.

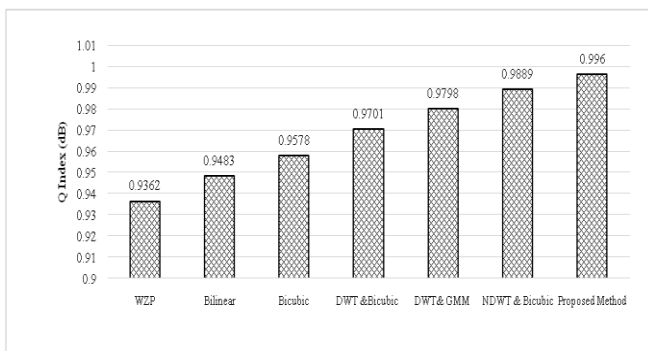


Figure 9 Q index for Satellite Image of Washington-DC.

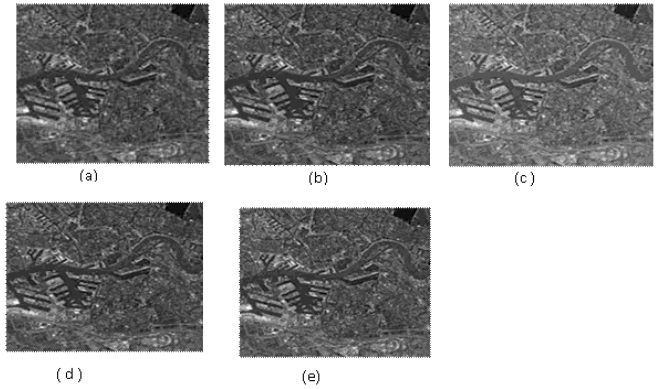


Figure 10 Satellite Images (a) original low resolution image, (b) DWT based decomposition and bi-cubic interpolated, (c) DWT based decomposition and GMM interpolated image, (d) NDWT based decomposition and bi-cubic interpolated Image and (e) NDWT based decomposition and GMM interpolated image.

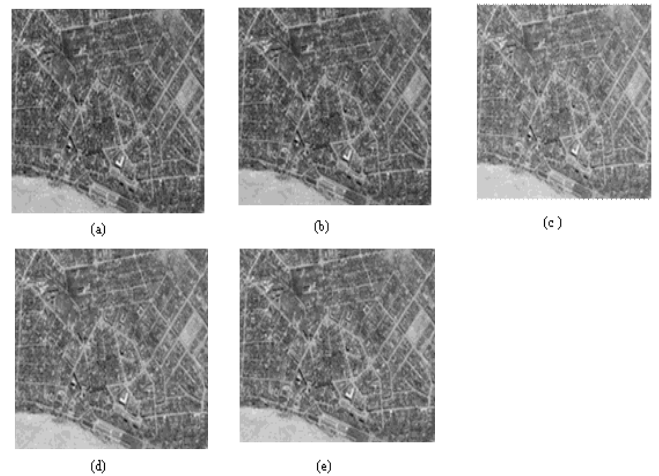


Figure 11 Satellite Images (a) original low resolution image, (b) DWT based decomposition and bi-cubic interpolated, (c) DWT based decomposition and GMM interpolated image, (d) NDWT based decomposition and bi-cubic interpolated Image and (e) NDWT based decomposition and GMM interpolated image.

## 5 Conclusion

A new Satellite image resolution improvement technique is achieved by using non-decimated wavelet transform to decompose the image and Gaussian Mixture Model interpolation to interpolate the coefficients. The results prove that the proposed technique is superior to existing methods. Image 1 is a Satellite Image of US-TOPO and Image 2 is a Satellite Image of Washington-DC was used for evaluating the methods. Table 1 lists the PSNR and Q Index achieved for the various techniques. To evaluate the proposed technique's performance, the original image was down sampled 50% on both the axes to obtain the down sampled image which is 1/4th size of the original image. After interpolation PSNR is computed using the original image as the base.



**Table 1: PSNR and QI results for proposed technique compared with conventional image resolution enhancement techniques.**

Technique	PSNR (dB)				Q Index			
	Image 1	Image 2	Image 3	Image 4	Image 1	Image 2	Image 3	Image 4
WZP	25.97	25.68	24.76	24.73	0.9362	0.9218	0.9289	0.9167
Bilinear	28.78	27.8	28.13	26.72	0.9483	0.9327	0.9434	0.9245
Bicubic	27.60	26.15	27.18	24.75	0.9578	0.9405	0.9506	0.9348
DWT & Bicubic	28.64	27.26	27.52	26.61	0.9701	0.9525	0.9654	0.9451
DWT & GMM	30.44	29.48	29.49	28.01	0.9798	0.9641	0.9742	0.96
NDWT & Bicubic	29.78	29.02	28.08	27.47	0.9889	0.9716	0.9833	0.9653
Proposed Method (NDWT & GMM)	32.49	31.92	31.85	30.66	0.996	0.9838	0.9874	0.9776

It is observed that the proposed NDWT and GMM method achieves higher PSNR and Q Index than the existing methods. The proposed method improves PSNR in the range of 6.52% to 22.31% compared to the existing techniques of image 1. Similarly for other images the proposed methods performs in a better way.

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